

**Seminar**  
**Discrete Mathematics**

**Title**  
**Lines, betweenness and metric spaces**

**Speaker**  
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**Abstract:**

A celebrated Theorem of de Bruijn and Erdos states that every noncollinear set of  $n$  points in the plane determines at least  $n$  distinct lines. Line  $uv$  in the plane consists of all points  $p$  such that:

- $\text{dist}(p,u) + \text{dist}(u,v) = \text{dist}(p,v)$  (i.e.  $u$  is between  $p$  and  $v$ ) or
- $\text{dist}(u,p) + \text{dist}(p,v) = \text{dist}(u,v)$  (i.e.  $p$  is between  $u$  and  $v$ ) or
- $\text{dist}(u,v) + \text{dist}(v,p) = \text{dist}(u,p)$  (i.e.  $v$  is between  $u$  and  $p$ ).

With this definition of line  $uv$  in an arbitrary metric space  $(V, \text{dist})$ , Chen and Chvatal conjectured that every metric space on  $n$  points, where  $n$  is at least 2, has at least  $n$  distinct lines or a line that consists of all  $n$  points. The talk will survey results supporting this conjecture as well as some discussions around lines induced by a set of points together with a betweenness relations. Most of the presented results can be found in "Lines, betweenness and metric spaces" (P.A., X. Chen, G. Huzhang, R. Kapadia, C. Supko).

Host: Marcos Kiwi

Date: Friday April 17, 2015 - 16:15.

Place: Sala de seminarios del CMM John Von Neumann.

